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Biomass equations for lodgepole pine in northern Sweden

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23 **Abstract**

24 Biomass equations for cultivated lodgepole pine (*Pinus contorta* var. *latifolia*) were developed
25 based on data from destructive biomass sampling of 164 trees collected from 13 sites at latitudes
26 61.9-66.2 °N in northern Sweden. Stand age varied between 20-87 years and top height between
27 8-32 m. Seeded and planted stands with different densities were included. Allometric biomass
28 equations for all above-stump components were constructed, expressing dry weight of stem,
29 bark, living and dead branch wood, foliage and cones, as well as total weight. Equations with 1-3
30 independent variables were constructed for each component, accounting variances within and
31 between sites. Estimated values for trees of different sizes were compared to corresponding
32 estimates for lodgepole pine in Canada and Scots pine in Sweden and Finland. Residual variation
33 of our equations was lower than that of equations from other sources. Our equations predicted
34 similar average biomass levels as Canadian equations for natural stands. In comparison to Scots
35 pine, at given stem dimensions, lodgepole pine had 50-100 % more foliage biomass and greater
36 dead branch biomass with increasing tree size. The wide amplitude of our data and the flexible
37 form of our equations should make them useful for wider application.

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39 *Keywords:* destructive biomass sampling, allometric functions

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45 1. Introduction

46 The growing market for bioenergy in the Nordic countries has targeted forest biomass as an
47 important feedstock (Ericsson et al. 2004). This, together with expectations relating to a future
48 bioeconomy (Octave and Thomas 2009) and carbon stock reporting under the Kyoto protocol,
49 has increased the need for tools to estimate the biomass carbon (C) stocks and energy assets of
50 forests. The C stock and energy assets are highly correlated with dry weight (DW) and can be
51 estimated with biomass equations. Such equations express the dry weight of different
52 components of the tree as a function of easily measured variables like diameter, height and
53 crown length. Different species differ with respect to wood density (Cannell 1989; Zobel and van
54 Buijtenen 1989) and allocation pattern. i.e. crown structure and stem form (Satoo and Madgwick
55 1982). Thus, separate functions are needed for each species. Biomass equations for Scots pine
56 (*Pinus sylvestris* L.), Norway spruce (*Picea abies* (L.) H. Karst) and birch (*Betula* spp.) in
57 Sweden and Finland have already been developed (Marklund 1988; Claesson et al. 2001;
58 Peterson and Ståhl 2006; Repola 2008; 2009; Repola and Ulvcróna 2014), but no equations are
59 available for lodgepole pine (*Pinus contorta* Dougl.).

60 As the inland form of lodgepole pine (*Pinus contorta* var. *latifolia*), introduced to Sweden from
61 western Canada on a large scale after 1970 (Elfving et al. 2001), starts to yield significant
62 amounts of biomass there is an urgent need for locally adapted biomass equations for this
63 species. Biomass equations for lodgepole pine are available (Brown 1978; Gholz et al. 1979;
64 Manning et al. 1984), but these equations are based on naturally regenerated trees from North
65 America, and until now the dominant method of regeneration in Sweden has been planting,

66 resulting in trees with different allocation of branches and foliage compared to naturally
67 regenerated ones (Long and Smith 1992; Litton et al. 2003).

68 In a review of available biomass equations, Ter-Mikaelian and Korzukhin (1997) reported two
69 individual studies with biomass equations for lodgepole pine from the grey literature (Brown
70 1978; Gholz et al. 1979). Both studies are limited in terms of number of sample trees/stands, tree
71 size and biomass fractions analyzed. In both studies three equations are presented i.e. for
72 stemwood including bark, needles and branches. The study by Brown (1978) is based on only
73 eight sample trees in the diameter range 1-5 cm. The study by Gholz et al. (1979) is limited to 29
74 sample trees with a diameter range from 3-29 cm. The grey literature also provides a larger study
75 by Manning et al. (1984), where biomass equations for lodgepole pine are presented for
76 stemwood, stem bark, branches (diam. > 0.5 cm), twigs (diam. < 0.5 cm) including foliage, and
77 for all above-stump biomass. The data behind the equations originated from 149 sample trees
78 collected from four ecoregions in the Yukon Territory with a diameter range between 3 and 36
79 cm. The limited information about site and stand characteristics, including regeneration method
80 and stem density, makes it difficult to judge whether these equations are useful for Swedish
81 conditions where most stands are regenerated by planting.

82 Based on a thorough review and published data on biomass equations for a number of North
83 American tree species, including lodgepole pine, Jenkins et al. (2003) developed generalized
84 biomass equations for conifers and broadleaves to be used for e.g. large scale inventory-based C
85 budgets. Their work was further developed by Chojnacky et al. (2014) and included an update of
86 published data. In both studies, pseudodata were generated within the diameter limitations of
87 published equations. The pseudodata were then used to construct generalized total biomass
88 equations over the full diameter range based on a two-parameter logarithmic regression model

89 with diameter at breast height (DBH) as the independent variable ($\ln(\text{biomass}) = \beta_0 + \beta_1 \times$
90 $\ln(\text{DBH})$). With all the uncertainties included in such an approach, Chojnacky et al. (2014)
91 concluded the need for better data to be collected across the distribution ranges of different tree
92 species and Jenkins et al. (2003) suggested a common protocol for biomass estimate studies and
93 that researchers, in addition to publishing their biomass equations, also published the data from
94 which their equations were developed.

95 Thus, despite inclusion of unpublished reports, we found few studies relating to lodgepole pine,
96 and those found were mostly based on few and small trees. No new, more comprehensive studies
97 have been found. It appears that there is a world-wide need for biomass equations for lodgepole
98 pine. Here we present such equations for different fractions of lodgepole pine trees based on 164
99 sample trees sampled in 13 stands in Sweden and we include the data behind the equations as an
100 appended Excel-file. The equations are compared with the equations published by Manning et al.
101 (1984) to indicate whether they could also be useful for estimates within the natural range of
102 lodgepole pine.

103

104 2. Material and methods

105 2.1 Site and stand descriptions

106 The sample trees were collected in northern Sweden, from latitude 61.9 °N in the south to
107 latitude 66.2 °N in the north (Figure 1, Table 1). Altitude varied between 80 and 440 metres
108 above sea level and stand age between 20 and 87 years. Number of stems ha^{-1} varied between
109 450 and 6034, basal area between 12 and 51 $\text{m}^2 \text{ha}^{-1}$ and top height between 8 and 32 m (Table
110 1). The distributions of sample trees over height- and diameter classes are given in Table 2.

111 Some sites hosted long-term yield plots in field experiments but sample trees were only affected
112 by applied treatments in two of them: the spacing trial 1209 at Långsjönäset and the scarification
113 trial 1544 at Degerön. At Långsjönäset the square spacings 1.1, 1.6, 2.0, 2.85 and 4.0 m were
114 represented and sample trees were selected from all spacings. At Degerön the treatments were
115 ordinary patch scarification and deep ploughing on a poor sediment of deep sand and the
116 sampling included both treatments. The sites Toböle 2 and Korseleberget represent the first
117 plantations of lodgepole pine in Sweden established in 1931 (Toböle 2) and 1928
118 (Korseleberget).

119

120 <Figure 1 here >

121 <Table 1 here>

122 <Table 2 here>

123

124 2.2 Sampling procedure

125 In total, 164 trees were sampled from 13 different sites during the years 1999-2012 (Table 1).

126 The same sampling procedure was applied in all but one study (Toböle 1999). First the main
127 procedure used is described and after that the deviations for the Toböle 1999 study.

128 Sample trees were selected by stratified (by DBH) random sampling among undamaged trees in
129 each plot. Forked trees and trees at stand borders were avoided. Diameter at breast height (DBH,
130 diameter over bark at 1.3 m above ground, cm) was marked and cross-callipered to the nearest
131 mm before felling. The aim of the biomass sampling was to estimate dry weight above ground,

132 and therefore each sample tree was cut down as close to the ground as possible. Measurements of
133 the felled trees included total stem length (L, m) and distance from stem base to the living crown,
134 defined as the lowest living branch separated from other living branches by less than three
135 whorls. Diameter was cross-callipered at the base of the stem, and at each metre up to the top.
136 The living crown was divided into four sections, each of which accounted for 25% of the crown
137 length (Figure 2). One branch ocularly judged to be representative of each section was selected
138 and cut using pruning shears. In addition, a representative dead branch was selected from below
139 the living crown of each sample tree. Stem discs (5 cm thick) were cut with a bow saw (scar
140 width 1.5 mm) or a chain saw (scar width 8 mm used for the larger trees) from the butt end of the
141 stem, at breast height (1.3 m), and at four positions representing 30, 55, 70 and 85% of the total
142 stem length (Figure 2). Scar widths were estimated by comparing the weight of some pieces of
143 wood before slicing with the different saws with the weight of the resulting discs. The saw-dust
144 lost with the chain saw was compensated for but not that from the bow saw. Directly after felling
145 and dividing a tree the sample discs and sample branches were weighed in the field on a
146 laboratory balance (6 kg maximum, ± 0.0005 kg) to obtain the fresh weight. The remaining stem
147 sections and all other branches from each section were weighed on a scale (30 kg maximum, \pm
148 0.002 kg). For the sampling in Toböle and Korseleberget in 2012, a scale with 100 kg maximum
149 was used for the remaining stem sections and branches. All sample branches and disc samples
150 for individual sample trees were put in separate airtight plastic bags and within 8 hours from the
151 time of tree felling, the samples were placed in a freezer (- 20 °C), where they were stored until it
152 was time to determine their dry weight .

153

154 <Figure 2 here>

155

156 The sectioning of the stem was used to estimate the stem volume and served as a back-up for
157 checking the stem form and weight. Stem volume over bark (V , dm^3) was estimated as:

158

$$159 \quad (1) \quad V = (\pi/4000) (\sum(d_i)^2 + 0.5 ((2d_0 + d_1)/3)^2)$$

160

161 where d_i is the diameter (mm) at the upper end of each 1-m stem section and d_0 is the
162 diameter at the lower end of the first section. This corresponds to Huber's formula
163 with addition of an approximation for the bottom half-meter section.

164 For nine of the sites (in total 119 sample trees) the bark was separated from the discs in the
165 laboratory, and both fractions were immediately weighed on a laboratory balance (6 kg
166 maximum, ± 0.0005 kg) to obtain separate fresh weights for the disc (wood) and the bark. Discs
167 and bark, or discs including the bark, were dried in a ventilated oven at 85°C for 48 hours before
168 measuring their dry weight. The discs were then further dried until their weight didn't decrease
169 any more. For living branches, foliage was separated from the branches after 24 hours of drying
170 in a ventilated oven (85°C), whereas the cones were combined with the branches. The different
171 fractions were then further dried for another 24 hours before weighing. Dead branches were
172 treated as one fraction without needles and were dried in a ventilated oven at 85°C for 48 hours
173 before measuring their dry weight.

174 Dry weights for biomass components (DW_x , kg dry weight per tree) were estimated from
175 measured data as follows, where all disc and section values include bark:

176 *Stem including bark* (DW_{stem})

177

$$178 \quad (2) \quad DW_{stem} = \sum \left(\frac{(DW_{disc\ i} + DW_{disc\ i+1})}{(FW_{disc\ i} + FW_{disc\ i+1})} \times FW_{stem\ section\ i} + DW_{disc\ i} \right)$$

179

180 where $DW_{disc\ i}$ is the dry weight of disc i , $FW_{disc\ i}$ is the fresh weight of disc i , $FW_{stem\ section\ i}$ is the fresh weight of the stem section with i in the range 1 to 6 including all
 181 stem sections from stump to top. For $i=6$ the index $i+1$ was reduced to 6.
 182

183 *Bark* (DW_{bark})

184

$$185 \quad (3) \quad DW_{bark} = \sum \left(\frac{(DW_{bark\ i} + DW_{bark\ i+1})}{(FW_{disc\ i} + FW_{disc\ i+1})} \times FW_{stem\ section\ i} + DW_{bark\ i} \right)$$

186

187 where $DW_{bark\ i}$ is dry weight of the bark of disc i . Other acronyms are as defined
 188 under equation (2).

189 *Living branches* (DW_{lbr})

190

$$191 \quad (4) \quad DW_{lbr} = \sum FW_{stratum.j} \times \left(\frac{DW_{sbw.j}}{FW_{sb.j}} \right)$$

192

193 where $FW_{stratum.j}$ is the fresh weight for stratum j including the sample branch, with j
 194 in the range 1-4. $DW_{sbw.j}$ is the dry weight of the sample of branch wood including
 195 cones and $FW_{sb.j}$ is the fresh weight of the sample branch.

196 *Foliage* (DW_{fol})

197

$$198 \quad (5) \quad DW_{fol} = \sum FW_{stratum.j} \times \left(\frac{DW_{sbf.j}}{FW_{sb.j}} \right)$$

199

200 where $DW_{sbf.j}$ is the dry weight of the foliage of the sample branch j , and other
 201 acronyms are as defined under equation (4).

202

203 *Dead branches* (DW_{dbr})

204

$$205 \quad (6) \quad DW_{dbr} = FW_{DB} \times \left(\frac{DW_{dsb}}{FW_{dsb}} \right)$$

206

207 where FW_{DB} is the total fresh weight of dead branches, DW_{dsb} is the dry weight of
 208 the dead sample branch and FW_{dsb} is the fresh weight of the dead sample branch.

209 *Cones* (DW_{cone})

210

$$211 \quad (7) \quad DW_{cone} = \sum FW_{stratum.j} \times \left(\frac{DW_{sbc.j}}{FW_{sbj}} \right)$$

212

213 where $DW_{sbc,j}$ is the dry weight of cones on the sample branch j and other acronyms
214 are as defined under equation (4).

215 For the Toböle site sampling in 1999, a slightly different sampling procedure was used (Elfving,
216 2002). Diameter at breast height was marked and cross-callipered to the nearest mm before
217 felling. Tree height was measured, and stump height was marked at 1 % of tree height before
218 felling. After felling, the length of the stem was measured. All dead branches were directly
219 gathered and weighted and a representative sample of about 1 kg was selected for dry weight
220 determination in the laboratory. All living branches were divided into branch fractions with and
221 without needles. Total fresh weight was determined for both groups, representative samples
222 (about 1 kg) were selected from each group and their fresh and dry weights were determined.
223 Stem discs 5 cm thick were cut at 1.5 m and then every 3 m up the stem. Drying of the samples
224 to determine dry weight followed the same procedure as above. Stem volume was estimated as
225 $3\pi/4$ times the sum of squared disc diameters, and stem biomass as volume times mean wood
226 density according to the basal area weighted mean of the stem discs.

227 By convention, stump height is generally defined as 1 % of tree height. In this study only the
228 length from stump to tree top on the felled tree (L , m) was measured (except at Toböle 1999
229 when tree height was measured for the standing tree). To ensure conformity with other studies,
230 measured data was adjusted as follows. Tree height above ground (H , m) was estimated as $H =$
231 $L/0.99$.

232 2.3 Statistics

233 Allometric biomass equations of the form $\ln(Y)=b_0 + b_1 \cdot \ln(x_1) + b_2 \cdot \ln(x_2) \dots$ were estimated for
234 dry weight (kg) of the total tree above-stump (DW_{tot}) and for the components stem with bark
235 (DW_{stem}), living branches (DW_{lbr}), dead branches (DW_{dbr}) and foliage (DW_{fol}) using the
236 procedure MIXED in the SAS statistical package. Two-three levels of equations were estimated
237 for each component including different numbers of explanatory variables: (1) only based on
238 DBH, (2) based on DBH and H, (3) based on DBH, H and crown length (crl). Appropriate forms
239 of the partial relationships were found by residual studies. The within and between site variation
240 was separated with the MIXED procedure, specifying site as a random class variable according
241 to the model:

$$242 \quad (8) \quad \ln Y_{ij} = b \times X_{ij} + u_j + e_{ij}$$

243 where Y_{ij} is measured biomass of actual component for tree i at site j , b is a vector of
244 coefficients, X_{ij} is a vector of explanatory variables, u_j is the random effect for site j and e_{ij} is
245 the random effect for tree i at site j . It is assumed that u_i and e_{ij} are un-correlated and have
246 normal distributions with mean=0. The error terms are model parameters which variances
247 are to be estimated.

248

249 For the partial relationship with DBH, the transformations $\ln(DBH)$ and $DBH/(DBH+x)$ were
250 tested, with a search process to find the most appropriate value of x for each biomass component.
251 The latter formulation was used by Marklund (1988) and Repola (2008, 2009) for Scots pine,
252 Norway spruce and birch ssp. biomass in Sweden and Finland. The differences were marginal for
253 our data and the first form was chosen since it performed well for all components. Tree height
254 was an important variable for estimating biomass of all components except that of dead branches

255 while crown length was important for estimating branch- and foliage biomass. To get an
256 appropriate partial relationship of stem biomass to height, both height ($\ln H$) and height above
257 breast height ($\ln(H-1.3)$) were included for this component as well as in the equation for total
258 biomass. The most commonly applied volume equations for pine and spruce in Sweden (Brandel
259 1990) also include this partial relationship of stem volume to height. Since stem biomass and
260 stem volume are closely related it seems as if this form of the relation between stem size and
261 height is quite general.

262 The variable $H/(\text{DBH})$ describes stem form (slenderness) and was more significant than $\ln(H)$
263 for estimating the foliage biomass. Since logarithmic transformation causes bias in the absolute
264 scale, the additive coefficients in the equations were adjusted by including the following
265 correction (adj), according to Snowdon (1991):

$$267 \quad (9) \quad \text{adj} = \ln(\Sigma \text{DW}_{\text{obs}}) - \ln(\Sigma \exp(\ln(\text{DW}_{\text{Eq}})))$$

269 where $\Sigma \text{DW}_{\text{obs}}$ is the sum of observed biomass of the actual component in absolute terms and
270 $\ln(\Sigma \text{DW}_{\text{Eq}})$ is the sum of the unadjusted values given by the equation. The intercepts in Table 3
271 have been corrected in this way.

272 Data on the fraction of bark biomass were only available for 119 trees from nine sites. Bark
273 biomass (DW_{bark}) was expressed as bark proportion (Bp) of the stem biomass
274 ($\text{Bp} = \text{DW}_{\text{bark}} / \text{DW}_{\text{stem}}$) and was studied as a function of DBH and H. The best correlation was
275 found with the transformed variable $1/(H+3)$. The variation in bark proportion within the stem
276 was also studied based on stem disc data. The dependent variable was then the bark proportion of

277 the disc biomass including bark ($B_{p_{disc}}$). The best model included a second-degree polynomial of
278 disc relative height position (H_{rel} , H_{rel}^2) and the transformed variable $1/(H+3)$. The variable
279 H_{rel} (h/H , where h is height above stump) is defined in the interval 0-1 where 0 is stump height
280 and 1 is tree top.

281 Since lodgepole pine often retains its cones for decades (Elfving et al. 2001), the cone biomass
282 can form a substantial part of the branch biomass. This amount was examined based on data
283 from 64 trees from five sites where the fresh and dry weights of cones were measured separately
284 from the branch samples. Since the appearance of cones was stochastic (several examined trees
285 lacked cones on the sample branches) a two-step model for estimation of cone biomass (DW_{cone})
286 was formulated. In step one the probability that there are no cones (plc) was estimated with a
287 logistic regression:

$$(10) \quad (\ln(1/plc-1)=b_0+b_1 \cdot (H/(DBH+1)))$$

288
289
290
291 where plc is probability that there are no cones on the sampled branches from a tree
292 and b_0 and b_1 are coefficients to be estimated.

293 In step two, the biomass of cones on trees with cones (DW_{c1}) was estimated with ordinary least
294 squares regression (OLS). Dry weight of cone biomass is estimated by combining the logistic
295 and OLS equations as:

$$(11) \quad DW_{cone} = DW_{c1} \times (1-plc)$$

298

299 The estimated stem volumes according to the sectioning were used to identify outliers in the
300 data. One stem was deleted since the stem weight and the sectioned volume did not correspond.
301 Two trees were outliers from the biomass equations and it was found that their DBH-values
302 deviated more than three times the expected measurement error from the stem profile according
303 to the sectioning. The original DBH-value was then replaced with the value estimated from the
304 stem profile curve.

305

306 3. Results

307 Equations for estimation of total tree biomass and for the tree components: stem with bark, living
308 branches with cones, foliage and dead branches are presented in Table 3. Equations for separate
309 estimation of bark proportion and the biomass of cones are presented in Table 4 and residuals in
310 relation to observed data are shown in Figures 3-4. All independent variables included in the
311 equations were highly significant ($p < 0.01$). Inspection of the residuals confirmed that they
312 fulfilled the assumptions done in the model formulation.

313

314 <Tables 3-4 and figures 3-4> here

315

316 4. Discussion

317 The data for this study came from cultivated stands older than 20 years with top heights above 7
318 m. The equations are therefore not valid for younger stands. Initial growing conditions have a
319 large impact on tree shape (Lindgren et al. 2007). The sample trees represent a wide variety of
320 growing conditions. The provenances used were all from the interior of Canada between latitudes
321 54 and 61°N and represent the provenances recommended for cultivation in northern Sweden.

322 Level 1-equations with only diameter as the independent variable had large residual variations,
323 with between-site variation as the dominant component. They are not recommended for practical
324 use but are included to demonstrate the increased efficiency of including more independent
325 variables. Inclusion of top height according to Table 3 in the model reduced the residual variance
326 substantially (calculation not shown). Stand height can be efficiently estimated by airborne laser
327 scanning (Nilsson et al. 2015) and should always be included in future large-scale biomass
328 estimations.

329 Our sampling was not focussed on a specific population of lodgepole pine. Instead we tried to
330 include stands with as many different conditions we could find regarding stands density,
331 developmental stages, site conditions etc. This means that we could expect a larger between-
332 stand residual variation than what is found in data from ordinary population sampling. For
333 example, at Örnåsen all biomass components except dead branches had lower biomass than
334 expected ($p < 0.01$) and at Degerön they were all higher than expected ($p < 0.001$). Also at
335 Korseleberget all components had more biomass than expected but the deviation had lower
336 significance ($p = 0.051$).

337 The sampling was spread over the snow-free season, from May to October (Tab. 1), which
338 influence the foliage biomass (DW_{fol}). If there are four fully developed age classes of needles at

339 the peak of DW_{fol} in late July and three classes left when the oldest class has been shed in late
340 autumn, the summer DW_{fol} would be about 30 % larger than the winter DW_{fol} . Our equations
341 probably give average values between those extremes. It should be noted that for single trees the
342 sum of predicted biomasses for different components generally deviates from the value predicted
343 by the equation for total biomass. The latter value is the best prediction of total biomass, and the
344 component sum can be brought into agreement with this value by proportional adjustment. In our
345 data the adjustment factor is in average 1.00 with the standard deviation 0.03. This adjustment
346 method is of course approximate. Different methods for additive modelling have been proposed,
347 restricting results from the partial relations to add up to the total (Parresol 2001, Poudel and
348 Temesgen 2016, Zhao et al 2016). Our aim was however to construct flexible partial equations
349 that can be used separately for different purposes. We did not try direct additive modelling but
350 our data are enclosed and can form a basis for further development of the modelling methods.

351 Results from this study were compared with predicted biomass for lodgepole pine in Canada
352 according to Manning et al (1984) and for Scots pine in Sweden and Finland according to
353 Marklund (1988) and Repola (2009), Table 5. The Canadian study was based on data from 149
354 lodgepole pine trees in the Yukon Territory. The Marklund study was based on data from 493
355 Scots pine trees forming a representative sample from the whole of Sweden, while the Repola
356 study was based on data from 908 Scots pine trees representing both research plots and ordinary
357 forests in Finland. The comparisons were conducted for small, medium and large trees with
358 central values of diameter and height according to Table 2 as independent variables.

359

360 <Table 5> here

361

362 The residual variation was smaller for the equations developed in this study than for the other
363 equations in the comparison (Table 5). One reason for this is probably smaller measurement
364 errors. The weighing of the whole tree used in this study gives high precision for the biomass
365 estimates. Another reason for smaller errors may be better specified partial relations.

366 In the Canadian study, residuals were given in absolute form and could not be translated to a
367 form comparable to the other studies. Instead the residuals presented here are those obtained
368 when we applied the Canadian model to our data. Living crown was split into larger branches
369 and twigs with foliage. Thus, comparable biomass components were stem with bark and living
370 tree crown. The Canadian values for dead branches refer to air-dry and not oven-dry weight.
371 For lodgepole pine, stem biomass was about 10 % larger according to the Canadian model than
372 according to our equation. This may be due to a higher wood density in the naturally regenerated
373 and dense stands in the Yukon, with slow-growing trees.

374 The Yukon values for living crown biomass (in average 71.7 kg according to table 5) are almost
375 equal to those in our study (in average 72.2 kg). For dead branches biomass the Yukon values are
376 14 % higher than our values. The higher Yukon values for dead branches depends probably on
377 moisture remaining in the air-dried branches. The fresh weight of dead branches was, on
378 average, 33 % higher than their dry weight in our data. This relationship varied between sites in
379 the interval 15-55 %, probably mostly related to the weather conditions before and during
380 sampling. In conclusion, the Canadian biomass equations by Manning et al (1984) seem to give
381 comparable biomass values as our equations.

382 The Canadian study included separate equations for stem biomass under bark and stem bark.
383 According to those equations, estimated bark proportion for the trees in Table 5 was about 20 %
384 higher than that estimated with the equation for bark proportion of stem dry weight in our study.
385 Cone biomass was also included in the branch biomass in the Canadian study and could not be
386 directly compared. At the five sites in our data where cones were separated they accounted for,
387 on average, 14 % of the branch biomass. Average dry weight per cone was 7.5 g.

388 For Scots pine, Marklund (1988) and Repola (2009) predict similar values for biomass of
389 different components. However, for large trees Repola (2009) predicts smaller dry weight for the
390 stem. The larger stem weight for Scots pine according to Marklund (1988) is almost the same as
391 for lodgepole pine according to this study. This looks like a coincidence, since both bark
392 thickness at breast height and probably also average wood density are larger for Scots pine than
393 for lodgepole pine. The higher wood density is because of the slower growth rate of Scots pine
394 on comparable sites, cf. Persson 1993. The most striking difference in biomass between
395 lodgepole pine and Scots pine concerns foliage and dead branches. Lodgepole pine is predicted
396 to have 50-100 % higher foliage biomass than Scots pine, while the proportion of dead branches
397 of total crown biomass is almost the same for small trees (20 %), but increases to 30 % in large
398 lodgepole pine and decreases to 15 % in large Scots pine. Those differences are certainly
399 species-specific.

400 The stump-root system was not included in this study. According to Marklund (1988) this
401 component constituted 20-25 % of the total tree biomass for both Scots pine and Norway spruce
402 of common tree sizes (DBH=6-25 cm, H=5-20 m). In this case, the stump-root system included
403 the roots that were still attached to the stump when the tree had been pulled down. The similarity

404 between pine and spruce in this aspect may indicate that similar values can be expected for
405 lodgepole pine.

406 Peterson and Ståhl (2006) examined the biomass of the smaller roots and found that the
407 Marklund (1988) values should be increased by 6 % to include all roots down to 5 mm and by 11
408 % to include all roots down to 2 mm. New functions based on an extended data-set were also
409 presented. It was found that the biomass of the stump-root systems were larger on moist than on
410 mesic and dry sites.

411 In conclusion the biomass equations presented for lodgepole pine had smaller residuals than
412 other comparable biomass equations for lodgepole pine and Scots pine, and estimated biomass in
413 different tree components deviated from these other equations as expected. The wide amplitude
414 of our data and the flexible form of our equations should make them useful for a wide range of
415 applications, both for detailed analyses at the single tree level and for large-scale estimates at the
416 stand- and forest levels.

417

418 Acknowledgements

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562

563 Table 1. Stand data, sample year and number of sample trees per site

<i>Site</i>	<i>Alt. (m)</i> <i>(a.s.l)</i>	<i>Age</i> <i>years</i>	<i>Top height</i> <i>(m)</i>	<i>Number of</i> <i>stems ha⁻¹</i>	<i>Basal area</i> <i>m² ha⁻¹</i>	<i>Sampling</i> <i>year-</i> <i>month</i>	<i>Number</i> <i>of sample</i> <i>trees</i>	<i>Experim.</i> <i>number/</i> <i>reference</i>
Örnåsen	370	26	14-16	1630-1790	27-31	2010-10	19	1156
Långträsk	260	31	13-14	1830-2080	26-28	2010-10	13	1155
Långsjönäset	360	40	15-18	500-6034	17-51	2008-05	29	1209
Kälvjärv	150	28	8-9	1053-1614	10-14	2005-10	20	Ref 1
Snägden	160	25	13	1725	24	2006-07	11	Ref 2
Rödmyrdalen	150	29	15	2320	36	2006-07	10	Ref 2
Toböle 1	80	48	19	860	28	1999-05	8	Ref 3
Toböle 1	80	61	26	610	30	2012-09	4	1113
Toböle 2	80	84	32	450	45	2012-09	4	1962
Korseleberget	350	87	28	540	34	2012-10	8	1959
Tönningstenen	440	29	9	3663	12	2011-09	2	Ref 4
Framsängsån	230	29	13	2338	29	2011-09	2	Ref 4
Bjärkliden	325	20	8	5000	21	2012-09	18	Ref 5
Degerön	150	27	10-12	2500	16-22	2012-09	16	Ref 6

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565 Note. Experiment numbers refer to the Swedish database Silva Boreal (2014) for forest field
 566 experiments. References: ref 1: Kero 2007; ref 2: Gardmo 2007; ref 3: Elfving 2002; ref 4:
 567 Backlund and Bergsten 2012; ref 5: Ulvcrona et al. 2013; ref 6: Egnell et al. 2015.

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574 Table 2. Distribution of biomass sample trees in the different height- and diameter classes.

575 Number of sample trees in each class.

<i>H-class</i>	<i>DBH class, cm</i>															Total	
m	4-6	-8	-10	-12	-14	-16	-18	-20	-22	-24	-26	-28	-30	-32	-34	-36	Total
4-6	1	2															3
-8		10	8	6	1												25
-10	1	4	3	12	4	1											25
-12		3	5	6	4	5	1										24
-14		2	2	2	4	9	4	4									27
-16			1	4	7	2	7	4	1	2							28
-18					2	3	1	3		1							10
-20					1	1		1	2								5
-22								1	2								3
-24								3				2			1		6
-26											1		2	1			4
-28															1		1
-30											1			1		1	3
Total	2	21	19	30	23	22	13	13	8	3	2	2	2	2	2	1	164

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585 Table 3. Biomass equations for lodgepole pine, giving the dry weight (DW, kg) of different
 586 components as a function of DBH over bark (DBH, cm), total tree height (H, m) and length of
 587 living crown (crl, m). The terms s^2_{sites} and s^2_{trees} denotes the residual variances between and
 588 within sites, and $Sres\text{-tot} = \sqrt{(s^2_{\text{sites}}+s^2_{\text{trees}})}$ is the total residual error of the equation. Standard
 589 errors of the coefficients are given in parenthesis below the coefficients

<i>Coefficients for independent variables</i>									
Dependent variable	Intercept ¹	ln(DBH)	ln(H)	ln(H-1.3)	H/DBH	ln(crl)	s^2_{sites}	s^2_{trees}	Sres-tot
All above stump: ln(DW _{tot})	-2.177 (0.089)	2.371 (0.028)					0.0320	0.0097	0.204
	-3.958 (0.336)	2.182 (0.033)	2.852 (0.840)	-2.062 (0.744)			0.0025	0.0075	0.100
Stem with bark: ln(DW _{stem})	-1.834 (0.138)	2.121 (0.035)					0.1379	0.0154	0.392
	-5.235 (0.281)	1.729 (0.026)	4.832 (0.690)	-3.265 (0.610)			0.0024	0.0045	0.083
Living branches: ln(DW _{lbr})	-7.665 (0.293)	3.601 (0.093)					0.3143	0.1108	0.652
	-4.619 (0.216)	4.269 (0.113)	-1.858 (0.141)				0.0086	0.0939	0.320
	-4.655 (0.208)	3.657 (0.133)	-1.967 (0.132)			0.940 (0.136)	0.0103	0.0718	0.287
Foliage ln(DW _{fol})	-5.642 (0.272)	2.717 (0.085)					0.3951	0.0912	0.697
	-1.708 (0.441)	1.759 (0.114)			-1.432 (0.168)		0.0368	0.0839	0.348
	-1.577 (0.404)	1.101 (0.149)			-1.547 (0.154)	0.834 (0.134)	0.0322	0.0677	0.316
Dead branches: ln(DW _{dbr})	-6.235 (0.349)	2.797 (0.120)					0.2321	0.1963	0.655
	-6.052	3.609				-1.138	0.163	0.171	0.577

(0.320) (0.188) (0.213)

590 ¹ Corrected for logarithmic bias

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594 Table 4. Equations for bark proportion of stem biomass and for cone biomass. H is the tree
595 height (m), H_{rel} is relative height (stump=0, top=1), DW_{c1} is dry weight of cones in branch
596 samples with cones, plc is the probability of cones being absent from the branch sample

597

<i>Dependent variable</i>	<i>Coefficients</i>							Adj. R ²	S _{res}	n
	Intercept	1/(H+3)	Hrel	(Hrel) ²	ln (H)	H/ (DBH+1)				
Bark prop. of DW _{stem}	0.0524	0.5073					0.437	0.0109	119	
Bark prp. of DW _{disc}	0.0418	0.7275	-0.1222	0.2350			0.722	0.0192	714	
ln (DW _{c1})	-0.1128				2.2768	-7.1103	0.610	1.087	54	
ln(1/plc-1)	14.63					-12.82			64	

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608 Table 5. Estimated biomass (kg per tree) of different tree components of three tree sizes
 609 according to equations from this study and from other studies. Figures in italics indicate residual
 610 standard deviation of the different equations

<i>Tree variables</i>		<i>Biomass component</i>					<i>Biomass component</i>				
DBH (cm)	H (m)	DW _{stem}	DW _{lbr}	DW _{fol}	DW _{dbr}	DW _{tot}	DW _{stem}	DW _{lbr}	DW _{fol}	DW _{dbr}	DW _{tot}
		lodgepole pine-this study					Scots pine-Marklund 1988				
S _{res}		<i>0.083</i>	<i>0.320</i>	<i>0.348</i>	<i>0.655</i>	<i>0.100</i>	<i>0.196</i>	<i>0.456</i>	<i>0.527</i>	<i>0.945</i>	-
7	9	8.0	0.7	0.9	0.5	10.4	7.8	1.4	0.6	0.4	10.2
15	15	53.8	6.8	5.0	3.8	72.0	54.6	9.6	3.2	2.0	69.4
30	25	351.5	50.4	22.5	26.6	452.5	340.7	38.8	10.3	6.4	396.2
		lodgepole pine-Manning et al 1984					Scots pine-Repola 2009				
S _{res}		<i>(0.10)¹</i>	<i>(0.70)</i>	<i>(0.60)</i>	<i>(0.59)</i>	<i>(0.14)¹</i>	<i>0.110</i>	<i>0.361</i>	<i>0.476</i>	<i>0.784</i>	<i>0.138</i>
7	9	8.5	1.0	1.7	0.3	11.5	8.2	0.9	0.6	0.4	10.2
15	15	59.0	6.0	5.9	4.6	75.6	55.4	6.9	3.3	2.2	69.4
30	25	388.2	38.7	33.0	33.1	493.1	309.7	37.8	11.4	10.2	374.3

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612 ¹ Values in parentheses are residuals when the Manning model is used with our data, that is use
 613 of D²H as the only independent variable for all components with OLS on our data.

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625 Figure legends

626 Figure 1. Map showing location of all sites for biomass sampling. Latitude and longitude are
627 given in degrees, minutes and seconds (WGS84).

628

629 Figure 2. The sampling procedure. In the field the raw weight was determined for 6 discs, 6 stem
630 sections (between discs), 4 living sample branches (one per strata), 4 living branch strata, 1 dead
631 sample branch, 1 dead-branch bunch. Discs and sample branches were brought to the lab for
632 drying and dry weight determination.

633

634 Figure 3. Observed and estimated bark proportion of stem biomass according to equations in
635 Table 4: in total for stems of different heights (upper diagram) and in stem discs at different
636 levels in the stem (lower diagram).

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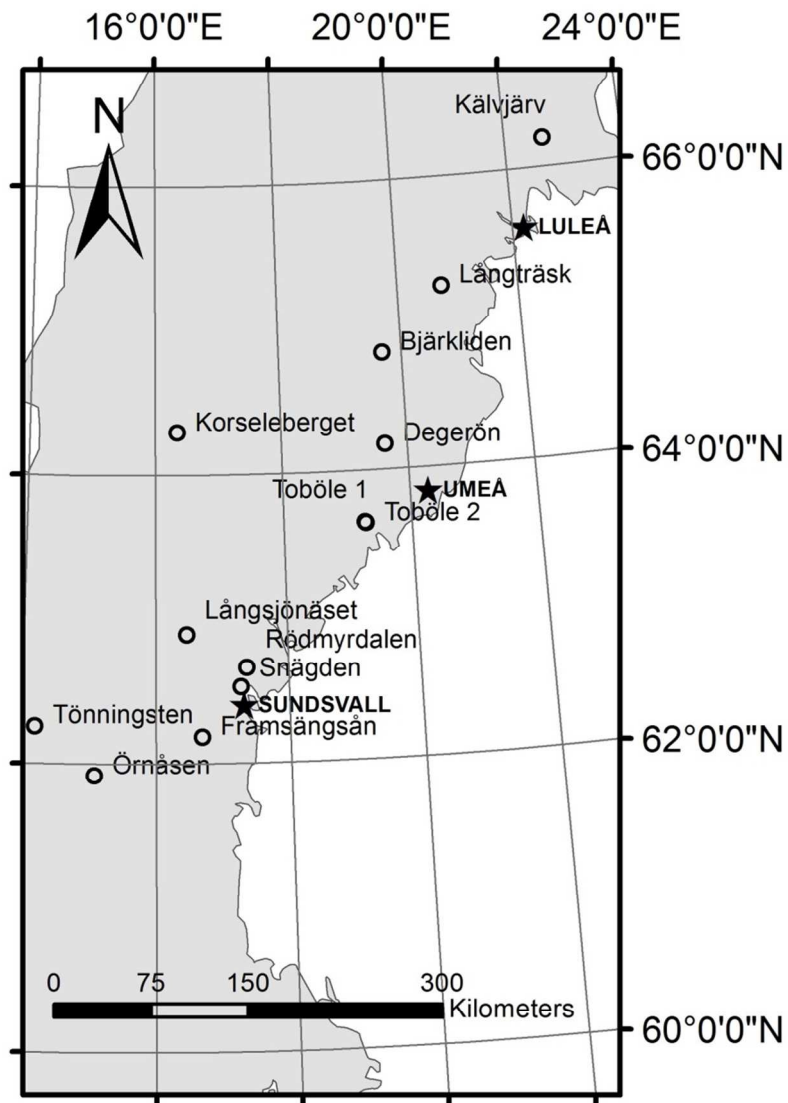
638 Figure 4. Observed and estimated cone biomass per tree according to the equations in Table 4.
639 Points mark mean observed values in different classes and figures are number of observations in
640 that class. The dashed line is the reference (regression).

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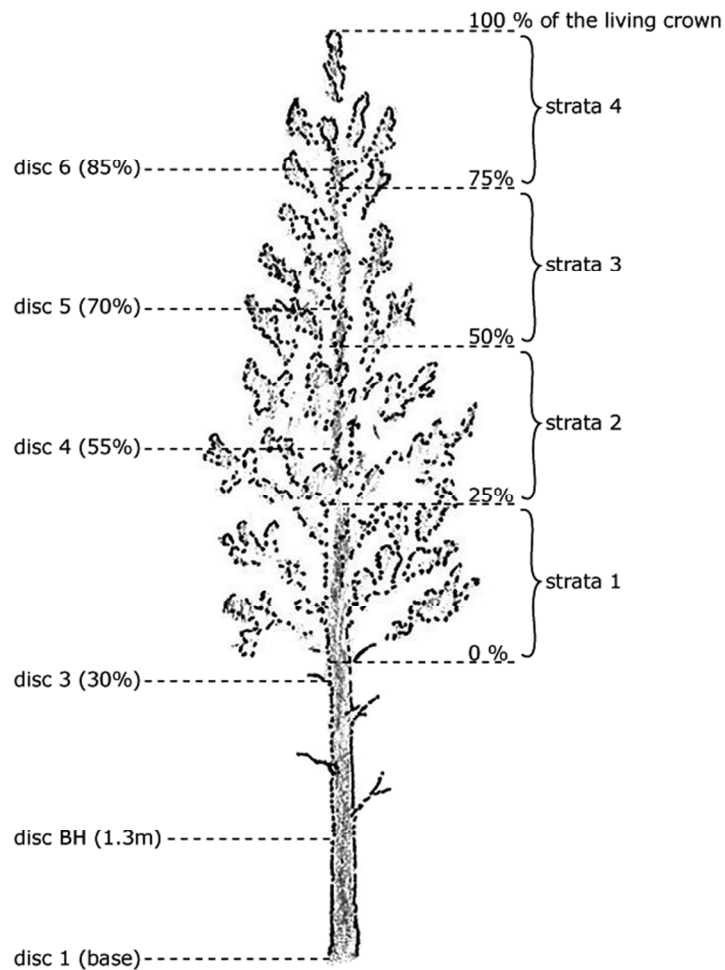
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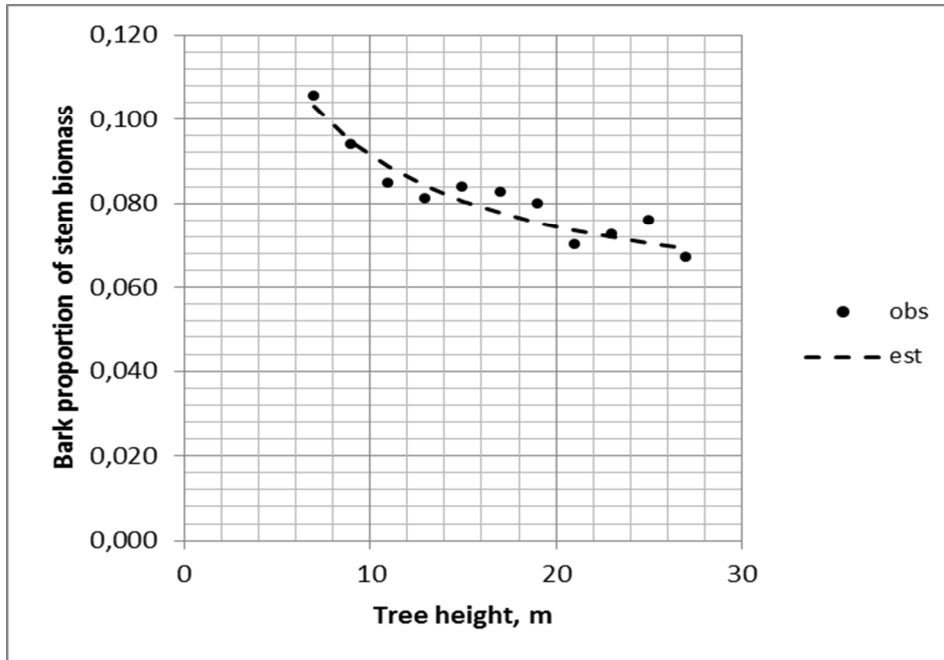
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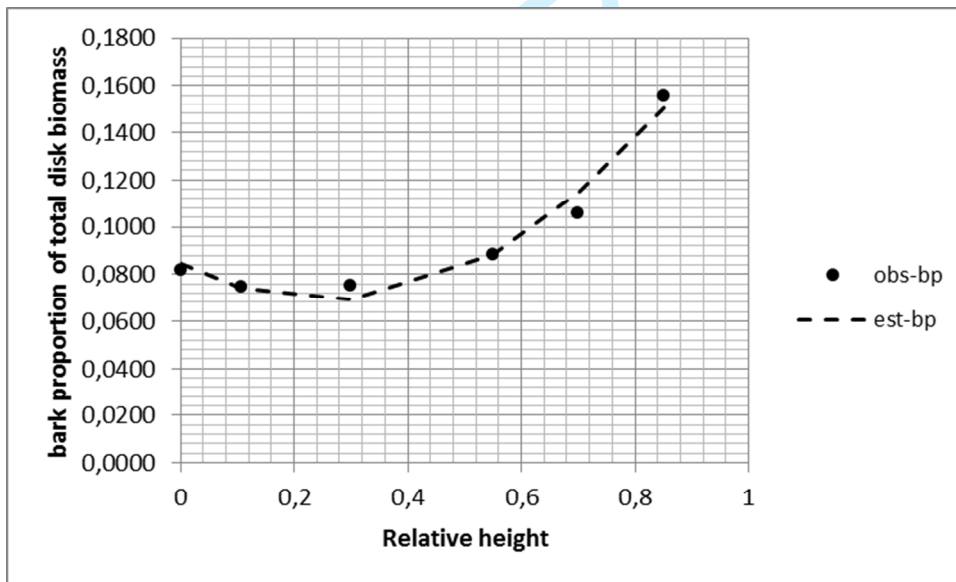
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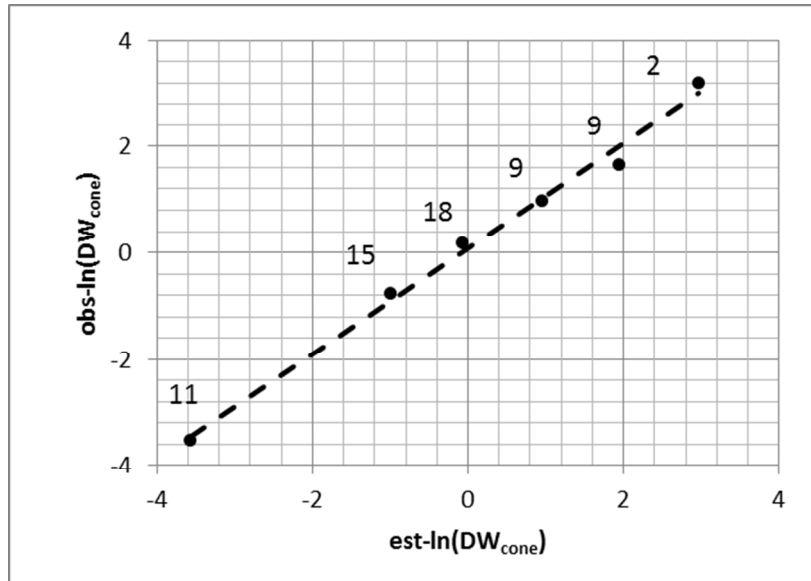
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Tönningstenen	440	29	9	3663	12	2011-09	2	Ref 4
Framsängsåsån	230	29	13	2338	29	2011-09	2	Ref 4
Bjärkliden	325	20	8	5000	21	2012-09	18	Ref 5
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Note. Experiment numbers refer to the Swedish database Silva Boreal (2014) for forest field experiments. References: ref 1: Kero 2007; ref 2: Gardmo 2007; ref 3: Elfving 2002; ref 4: Backlund and Bergsten 2012; ref 5: Ulvcróna et al. 2013; ref 6: Egnell et al. 2015.

Table 2. Distribution of biomass sample trees in the different height- and diameter classes.
Number of sample trees in each class.

<i>H-class</i>	<i>DBH class, cm</i>																Total
m	4-6	-8	-10	-12	-14	-16	-18	-20	-22	-24	-26	-28	-30	-32	-34	-36	
4-6	1	2															3
-8		10	8	6	1												25
-10	1	4	3	12	4	1											25
-12		3	5	6	4	5	1										24
-14		2	2	2	4	9	4	4									27
-16			1	4	7	2	7	4	1	2							28
-18					2	3	1	3		1							10
-20					1	1		1	2								5
-22								1	2								3
-24									3			2			1		6
-26											1		2	1			4
-28															1		1
-30											1			1		1	3
Total	2	21	19	30	23	22	13	13	8	3	2	2	2	2	2	1	164

Table 3. Biomass equations for lodgepole pine, giving the dry weight (DW, kg) of different components as a function of DBH over bark (DBH, cm), total tree height (H, m) and length of living crown (crl, m). The terms s^2_{sites} and s^2_{trees} denotes the residual variances between and within sites, and $Sres-tot = \sqrt{(s^2_{sites}+s^2_{trees})}$ is the total residual error of the equation. Standard errors of the coefficients are given in parenthesis below the coefficients

<i>Coefficients for independent variables</i>									
Dependent variable	Intercept ¹	ln(DBH)	ln(H)	ln(H-1.3)	H/ DBH	ln(crl)	s^2_{sites}	s^2_{trees}	Sres-tot
All above stump: ln(DW _{tot})	-2.177 (0.089)	2.371 (0.028)					0.0320	0.0097	0.204
	-3.958 (0.336)	2.182 (0.033)	2.852 (0.840)	-2.062 (0.744)			0.0025	0.0075	0.100
Stem with bark: ln(DW _{stem})	-1.834 (0.138)	2.121 (0.035)					0.1379	0.0154	0.392
	-5.235 (0.281)	1.729 (0.026)	4.832 (0.690)	-3.265 (0.610)			0.0024	0.0045	0.083
Living branches: ln(DW _{lbr})	-7.665 (0.293)	3.601 (0.093)					0.3143	0.1108	0.652
	-4.619 (0.216)	4.269 (0.113)	-1.858 (0.141)				0.0086	0.0939	0.320
	-4.655 (0.208)	3.657 (0.133)	-1.967 (0.132)			0.940 (0.136)	0.0103	0.0718	0.287
Foliage ln(DW _{fol})	-5.642 (0.272)	2.717 (0.085)					0.3951	0.0912	0.697
	-1.708 (0.441)	1.759 (0.114)			-1.432 (0.168)		0.0368	0.0839	0.348
	-1.577 (0.404)	1.101 (0.149)			-1.547 (0.154)	0.834 (0.134)	0.0322	0.0677	0.316
Dead branches: ln(DW _{dbr})	-6.235 (0.349)	2.797 (0.120)					0.2321	0.1963	0.655
	-6.052 (0.320)	3.609 (0.188)				-1.138 (0.213)	0.163	0.171	0.577

¹ Corrected for logarithmic bias

Table 4. Equations for bark proportion of stem biomass and for cone biomass. H is the tree height (m), H_{rel} is relative height (stump=0, top=1), DW_{cl} is dry weight of cones in branch samples with cones, plc is the probability of cones being absent from the branch sample

<i>Dependent variable</i>	<i>Coefficients</i>							Adj. R^2	S_{res}	n
	Intercept	$1/(H+3)$	Hrel	$(Hrel)^2$	ln (H)	H/ (DBH+1)				
Bark prop. of DW_{stem}	0.0524	0.5073					0.437	0.0109	119	
Bark prp. of DW_{disc}	0.0418	0.7275	-0.1222	0.2350			0.722	0.0192	714	
ln (DW_{cl})	-0.1128				2.2768	-7.1103	0.610	1.087	54	
ln(1/plc-1)	14.63					-12.82			64	

Table 5. Estimated biomass (kg per tree) of different tree components of three tree sizes according to equations from this study and from other studies. Figures in italics indicate residual standard deviation of the different equations

<i>Tree variables</i>		<i>Biomass component</i>					<i>Biomass component</i>				
DBH (cm)	H (m)	DW _{stem}	DW _{lbr}	DW _{fol}	DW _{dbr}	DW _{tot}	DW _{stem}	DW _{lbr}	DW _{fol}	DW _{dbr}	DW _{tot}
		lodgepole pine-this study					Scots pine-Marklund 1988				
S _{res}		<i>0.083</i>	<i>0.316</i>	<i>0.348</i>	<i>0.629</i>	<i>0.100</i>	<i>0.196</i>	<i>0.456</i>	<i>0.527</i>	<i>0.945</i>	-
7	9	8.0	0.7	0.9	0.5	10.4	7.8	1.4	0.6	0.4	10.2
15	15	53.8	6.8	5.0	3.8	72.0	54.6	9.6	3.2	2.0	69.4
30	25	351.5	50.4	22.5	26.6	452.5	340.7	38.8	10.3	6.4	396.2
		lodgepole pine-Manning et al 1984					Scots pine-Repola 2009				
S _{res}		<i>(0.10)¹</i>	<i>(0.70)</i>	<i>(0.60)</i>	<i>(0.61)</i>	<i>(0.14)¹</i>	<i>0.110</i>	<i>0.361</i>	<i>0.476</i>	<i>0.784</i>	<i>0.138</i>
7	9	8.5	1.0	1.7	0.3	11.5	8.2	0.9	0.6	0.4	10.2
15	15	59.0	6.0	5.9	4.6	75.6	55.4	6.9	3.3	2.2	69.4
30	25	388.2	38.7	33.0	33.1	493.1	309.7	37.8	11.4	10.2	374.3

¹ Values in parentheses are residuals when the Manning model is used with our data, that is use of D²H as the only independent variable for all components with OLS on our data

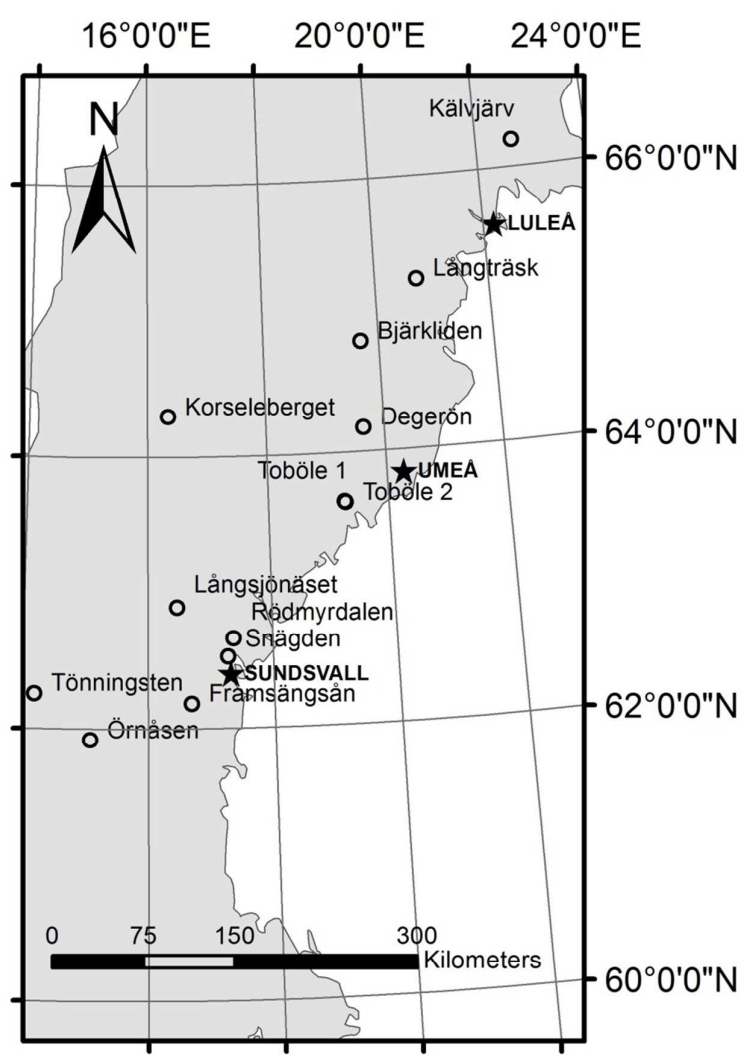


Fig. 1

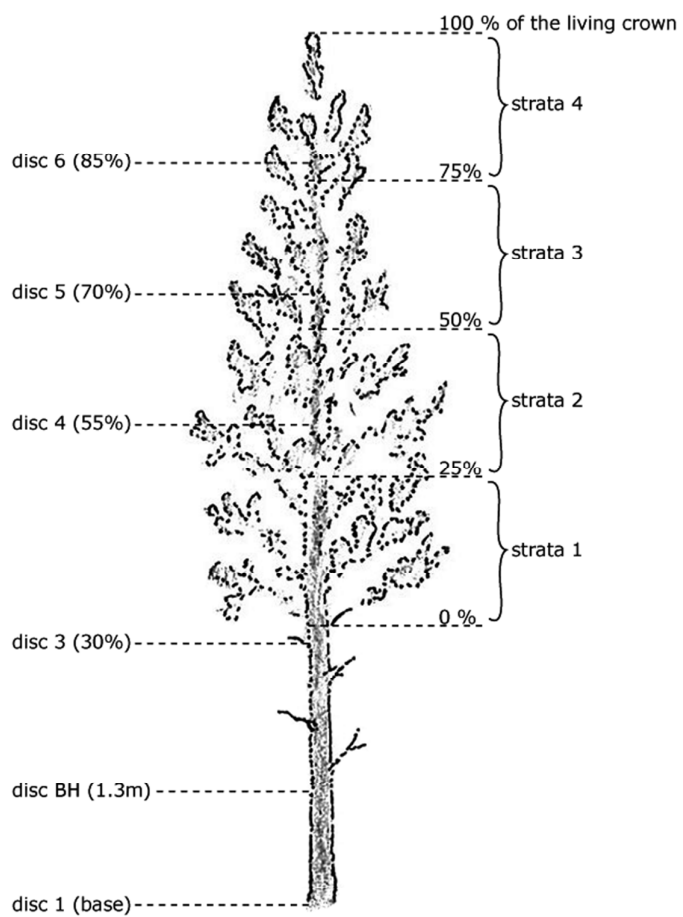


Fig. 2

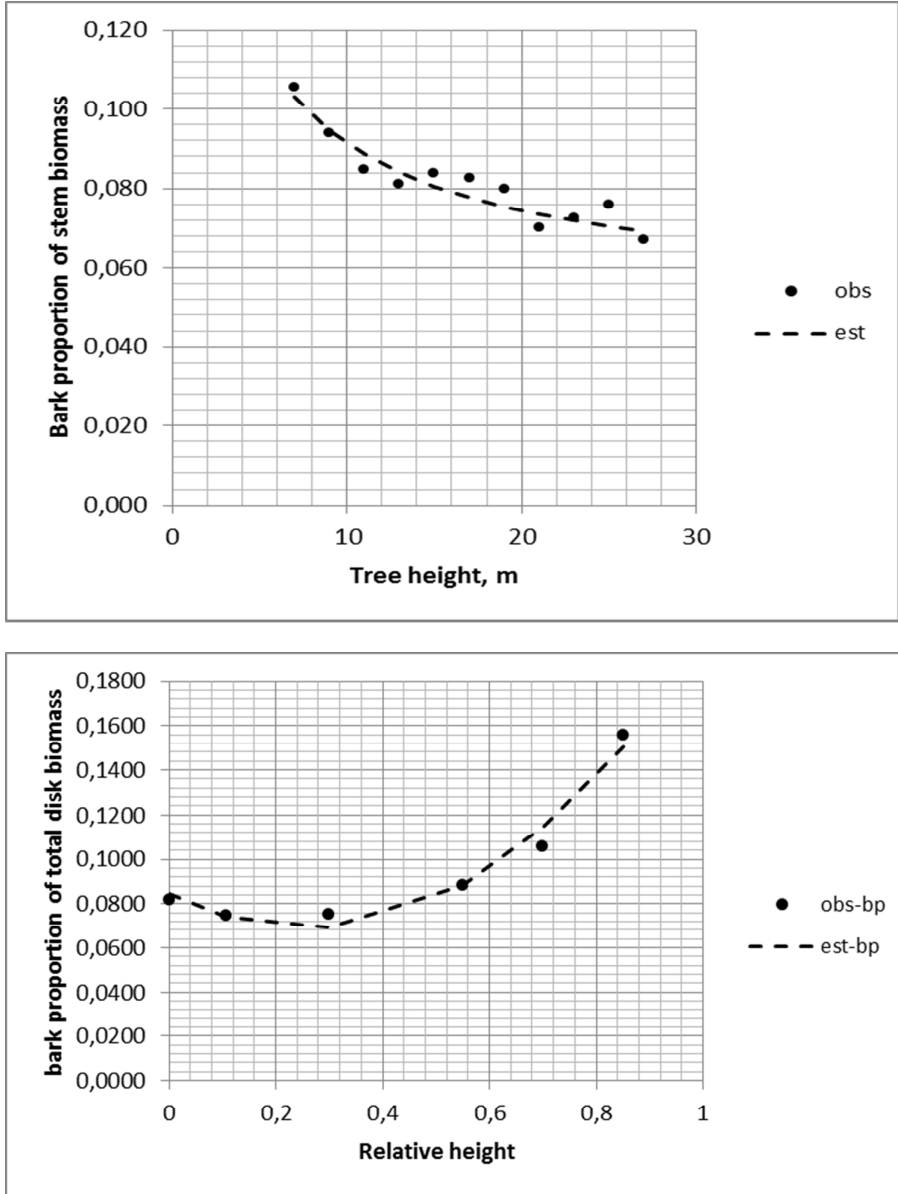


Fig. 3

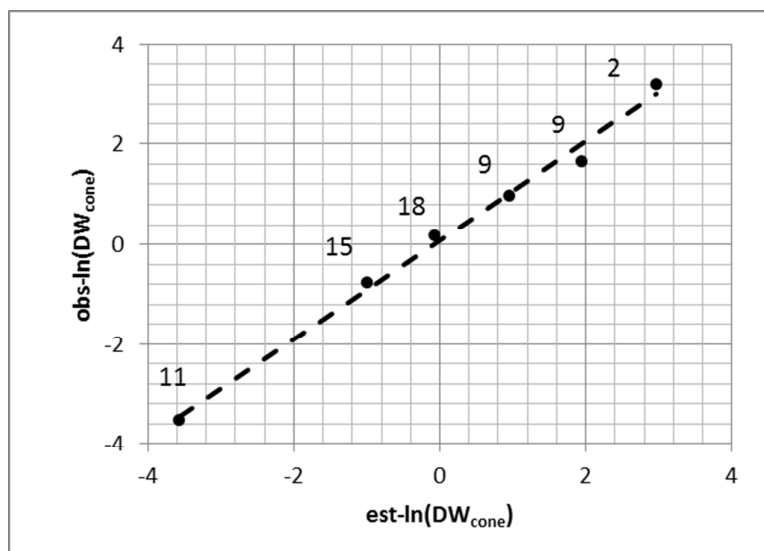


Fig. 4

Draft